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# Ground States of Molecules. 39. MNDO Results for Molecules Containing Hydrogen, Carbon, Nitrogen, and Oxygen 

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#### Abstract

Heats of formation, molecular geometries, ionization potentials, and dipole moments are calculated by the MNDO method for a large number of molecules. The MNDO results are compared with the corresponding MINDO $/ 3$ results on a statistical basis. For the properties investigated, the mean absolute errors in MNDO are uniformly smaller than those in MINDO/3 by a factor of about 2. Major improvements of MNDO over MINDO/3 are found for heats of formation of unsaturated systems and molecules with NN bonds, for bond angles, for higher ionization potentials, and for dipole moments of compounds with heteroatoms.


## (I) Introduction

In the preceding paper, ${ }^{1}$ we have introduced the approximations and parameters of the MNDO method (modified neglect of diatomic overlap). Here we report MNDO results for heats of formation, molecular geometries, ionization potentials, and dipole moments of a large number of molecules and compare them with the corresponding MINDO/ 3 values. ${ }^{2}$ All results in this paper were derived from single-determinantal MNDO calculations, without inclusion of configuration interaction ( Cl ), and refer to molecular structures optimized by the Davidon-Fletcher-Powell method. ${ }^{3}$

## (II) Heats of Formation

Tables I and II compare calculated and observed heats of formation for a set of 138 closed shell molecules, selected to represent as many bonding situations as possible and with emphasis on those which had presented problems in MINDO. The mean absolute error for these compounds is reduced from $11.0 \mathrm{kcal} / \mathrm{mol}$ in MINDO/3 to $6.3 \mathrm{kcal} / \mathrm{mol}$ in MNDO.

Here, and subsequently, we use average errors as a measure of accuracy, rather than standard deviations, because our compounds were not chosen at random. Indeed, in view of our deliberate inclusion of molecules that had proved especially "difficult" in previous studies, the errors reported here are certainly greater than they would have been for a randomly chosen set.

The main improvements of MNDO over MINDO/3, are found (Table I) in the case of aromatic systems, molecules with triple bonds ( $\mathrm{C} \equiv \mathrm{C}, \mathrm{C} \equiv \mathrm{N}$ ), three-membered rings, globular polycylic compounds with five- or six-membered rings, and molecules with NN bonds. Some of these improvements (e.g., for unsaturated systems and NN bonds) are probably due to the inclusion of directional effects in the two-center MNDO electron-electron repulsions and core-electron attractions. ${ }^{1}$

Large errors in the MNDO heats of formation (10-20 $\mathrm{kcal} / \mathrm{mol}$ ) are encountered in three areas where MINDO/3 met with similar difficulties. Four-membered rings are consistently predicted too stable and sterically crowded molecules
with adjacent methyl groups (e.g., tert-butyl compounds) too unstable, while molecules with NO bonds show errors in both directions. The first two shortcomings (four-membered rings, sterically crowded molecules) seem to be inherent in the basic

Table I. Mean Absolute Errors $\Delta\left(\Delta H_{\mathrm{f}}\right)$ for Heats of Formation ${ }^{a}$

|  | $\Delta\left(\Delta H_{f}\right), \mathrm{kcal} / \mathrm{mol}$ |  |  |
| :--- | ---: | ---: | ---: |
| Class of compd | No. | MNDO | MINDO/3 |
| All compounds | 138 | 6.3 | 11.0 |
| Hydrocarbons | 58 | 6.0 | 9.7 |
| With aromatic rings | 5 | 1.7 | 12.1 |
| With triple bonds | 6 | 6.6 | 13.5 |
| With three-membered rings ${ }^{b}$ | 8 | 5.2 | 11.7 |
| With four-membered rings ${ }^{b}$ | 7 | 18.7 c | 8.6 |
| Acyclic hydrocarbons | 26 | 3.5 | 6.9 |
| Cyclic hydrocarbons | 32 | 8.0 | 11.9 |
| Bicyclic hydrocarbons with 5. | 5 | 2.9 | 22.3 |
| and 6-membered rings |  |  |  |
| Nitrogen compounds (CHN) | 34 | 6.5 | 17.3 |
| Amines | 11 | 4.1 | 6.9 |
| Cyanides | 8 | 4.6 | 19.6 |
| With NN bonds | 11 | 8.1 | 29.5 |
| Oxygen compounds (CHO) | 39 | 5.2 | 6.8 |
| Alcohols, ethers | 12 | 4.3 | 5.7 |
| Aldehydes, ketones | 10 | 4.3 | 6.1 |
| Acids, esters, anhydrides | 9 | 3.2 | 6.8 |
| With OO bonds | 5 | 7.7 | 3.4 |
| Nitrogen-oxygen compounds | 7 | 14.8 | 15.4 |
| (CHNO) |  |  |  |
| All compounds excluding those | 122 | 5.0 | 10.9 |
| with 4-nembered rings, |  |  |  |
| tert-butyl groups, |  |  |  |
| or NO bonds |  |  |  |

${ }^{a}$ Based on the results in Table II. ${ }^{b}$ Including bicyclic compounds. Molecules containing three- and four-membered rings were counted in the class of four-membered rings only. ${ }^{c}$ Excluding cubane, the mean absolute error reduces to $13.5 \mathrm{kcal} / \mathrm{mol}$.

| Molecule | $\Delta H_{\mathrm{f}}, \mathrm{kcal} / \mathrm{mol}$ |  |  | Ref | Molecule | $\Delta H_{\mathrm{f}}, \mathrm{kcal} / \mathrm{mol}$ |  |  | Ref |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Calcd | Exptl | Error |  |  | Calcd | Expt1 | Error |  |
| $\mathrm{C}_{2} \mathrm{H}_{6}$ | -19.7 | -20.2 | +0.5 | $a$ |  |  |  |  |  |
| $\mathrm{C}_{2} \mathrm{H}_{4}$ | 15.3 | 12.5 | +2.8 | $a$ | (O) | 37.5 | 35.3 | +2.2 | $a$ |
| $\mathrm{C}_{2} \mathrm{H}_{2}$ | 57.3 | 54.3 | +3.0 | a |  |  |  |  |  |
| $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | -24.9 | -24.8 | -0.1 | $a$ | 7 | 33.6 | 43.9 | -10.3 | $a$ |
| $\mathrm{CH}_{3} \mathrm{CH}=\mathrm{CH}_{2}$ | 4.9 40.9 | 4.9 | 0.0 | $a$ | $\triangle$ | 33.6 | 43.9 | -10.3 | $a$ |
| $\mathrm{CH}_{3} \mathrm{C}=\mathrm{CH}$ | 40.9 | 44.4 | -3.5 | $a$ |  |  |  |  |  |
| $\mathrm{CH}_{2}=\mathrm{C}=\mathrm{CH}_{2}$ | 43.8 | 45.6 | -1.8 | $a$ | 人 | 69.1 | 51.9 | +17.2 | $a$ |
| $N$ | -29.7 | -30.4 | +0.7 | $a$ |  | 33.7 | 44.3 | -10.6 | $a$ |
| $\rangle$ | -26.8 | -32.4 | +5.6 | $a$ | N- | 33.7 28.6 | 30.9 | -10.6 -2.3 | $a$ |
| N | 0.3 | -0.2 | +0.5 | $a$ |  |  |  |  | $a$ |
| $\mathbb{N}$ | -5.1 | -3.0 | -2.1 | $a$ | $\square$ | 30.2 | 37.3 | -7.1 | $c$ |
| $\Gamma$ | -4.0 | -1.9 | -2.1 | $a$ |  |  |  |  |  |
| $=$ | -2.1 | -4.3 | +2.2 | $a$ | 1 | -10.3 | -12.4 | +2.1 | $e$ |
| $=1$ | 33.4 | 38.8 | -5.4 | $a$ |  | 62.6 | 59.7 | +2.9 | $c$ |
| N | 28.9 | 26.0 | +2.9 | $a$ |  |  |  |  |  |
| =1-1 | 35.6 | 39.5 | -3.9 | $a$ |  | -26.3 | -24.1 | -2.2 | $e$ |
| - $=$ | 24.4 | 34.7 | -10.3 | $a$ |  |  |  |  |  |
| =- | 65.0 | 72.8 | -7.8 | $b$ |  | 38.1 | 36.1 | +2.0 | $a$ |
| 一= | 102.2 | 113.0 | -10.8 | $b$ | - | 38.1 | 36.1 | +2.0 | $a$ |
| $\cdots$ | -34.4 | -35.1 | +0.7 | $a$ | Adamantane | -26.4 | -31.9 | +5.5 | $f$ |
| $+$ | -24.6 | -40.3 | +15.7 | $a$ | Cubane | 99.1 | 148.7 | -49.6 | $a$ |
| N | 18.7 | 18.1 | +0.6 | $a$ | $\mathrm{N}_{2} \mathrm{NH}_{3}$ | 8.0 -6.3 | 0.0 -11.0 | +8.0 +4.7 |  |
|  | 20.0 |  |  |  | $\mathrm{CH}_{3} \mathrm{NH}_{2}$ | -7.5 | -5.5 | -2.0 | $a$ |
| - | 20.0 | 19.1 | +0.9 | $a$ | $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH}$ | -6.6 | -4.4 | -2.2 | a |
| N | 25.9 | 25.3 | +0.6 | $a$ | $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{~N}$ | -2.8 | -5.7 | +2.9 | $a$ |
|  |  |  |  |  | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NH}_{2}$ | -12.9 | -11.4 | -1.5 | $a$ |
| $D$ | 11.2 | 12.7 | -1.5 | $a$ | $n-\mathrm{C}_{3} \mathrm{H}_{3} \mathrm{NH}_{2}$ | -17.9 | -16.8 | -1.1 | $a$ |
|  |  |  |  |  | $i . \mathrm{C}_{3} \mathrm{H}_{7} \mathrm{NH}_{2}$ | -16.0 | -20.0 | +4.0 | $a$ |
| $D$ cis | -1.8 | 1.3 | -3.1 | $c$ | $t-\mathrm{C}_{3} \mathrm{H}_{7} \mathrm{NH}_{2}$ | -15.1 | -28.9 | +13.8 | $a$ |
| 1 | 68.2 | 66.2 | +2.0 | $a$ | Dnh | 25.2 | 30.2 | -5.0 | $a$ |
| D | 53.6 | 58.2 | -4.6 | $a$ | - | 32.4 | 25.9 | +6.5 | $a$ |
|  | 39.1 | 46.4 | -7.3 | 6 | $\widehat{O}$ | 28.7 | 34.6 | -5.9 | $a$ |
| $D=$ | 37.8 | 47.9 | -10.1 | $a$ | ON | 44.2 | 66.5 | -22.3 | $a$ |
| $\square$ | -11.9 | 6.8 | -18.7 | $a$ |  |  |  |  |  |
| $\square$ | 31.0 | 37.5 | -6.5 | c | <- | 35.5 | 47.0 | -11.5 | $a$ |
| $\square$ | 6.4 | 19.8 | -13.4 | $c$ | $\stackrel{N}{\mathrm{~N}}$ | 38.3 | 46.9 | -8.6 | $a$ |
| $\bigcirc$ | 10.9 | 29.1 | -18.2 | $d$ |  | 22.0 | 20.8 | +1.2 | $a$ |
| $\square$ | -30.5 | -18.4 | -12.1 | $a$ | HCN | 34.9 | 32.3 | +2.6 | $g$ |
|  |  |  |  |  | $\mathrm{CH}_{3} \mathrm{CN}$ | 18.9 | 20.9 | -2.0 | $h$ |
|  | -0.4 | 8.2 | -8.6 | $a$ | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{CN}$ | 13.4 | 12.1 | +1.3 | $b$ |
|  |  |  |  |  | $\mathrm{CH}_{2}=\mathrm{CH}-\mathrm{CN}$ | 43.7 | 44.1 | -0.4 | $a$ |
|  | 32.0 | 31.9 | +0.1 | $a$ | $\sim^{\mathrm{CN}}$ | 74.6 | 81.3 | -6.7 | $a$ |
| $\square=$ | 53.6 | 47.5 | +6.1 | $a$ | $\mathrm{NC}-\mathrm{C} \equiv \mathrm{C}-\mathrm{CN}$ | 110.7 | 126.5 | -15.8 | $a$ |
|  |  |  |  |  | (CN) 2 | 65.9 | 73.8 | -7.9 | $a$ |
|  | -34.8 | -29.5 | -5.3 | $a$ | (O)- CN | 51.8 | 51.5 | +0.3 | $a$ |
| $\square$ | -10.0 | -1.1 | -8.9 | $a$ | $\mathrm{CH}_{3} \mathrm{NC}$ | 60.0 | 35.6 | +24.4 | $h$ |
|  |  |  |  |  | $\mathrm{NH}_{2}-\mathrm{NH}_{2}$ | 14.3 | 22.8 | -8.5 | 8 |
| $\Leftrightarrow$ | 14.4 | 25.4 | -11.0 | $a$ | $\mathrm{CH}_{3} \mathrm{NH}-\mathrm{NH}_{2}$ | 16.6 | 22.6 | -6.0 | $a$ |
|  |  |  |  |  | $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{~N}-\mathrm{NH}_{2}$ | 19.1 | 20.0 | -0.9 | $a$ |
| ( 0 | 21.2 | 19.8 | +1.4 | $a$ | $\mathrm{CH}_{3} \mathrm{NH}-\mathrm{NHCH}_{3}$ | 15.8 | 22.0 | -6.2 | $a$ |
|  | 13.5 | 12.0 | +1.5 | $a$ |  | 33.8 | 50.9 | -17.1 | $g$ |

Table II (Contimued)

| Molecule | $\Delta H_{\mathrm{f}}, \mathrm{kcal} / \mathrm{mol}$ |  |  | Ref | Molecule | $\Delta H_{\mathrm{f}}, \mathrm{kcal} / \mathrm{mol}$ |  |  | Ref |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Calcd | Exptl | Error |  |  | Calcd | Exptl | Error |  |
|  | 2.2 | 8.6 | $-6.4$ | $i$ | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{CHO}$ | -48.1 | -45.5 | -2.6 | $a$ |
|  |  |  |  |  | $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CO}$ | -49.5 | -51.9 | +2.4 | $a$ |
|  |  |  |  |  | $\mathrm{CH}_{2} \mathrm{CO}$ | $-7.0$ | -11.4 | +4.4 | $m$ |
| $\mathrm{CH}_{2} \mathrm{~N}_{2}$ | 67.1 | 71 | -3.9 | $j$ | $(\mathrm{CHO})_{2}$ | $-61.6$ | $-50.7$ | $-10.9$ | $a$ |
|  |  |  |  |  | $\left(\mathrm{CH}_{3} \mathrm{CO}\right)_{2}$ | -78.9 | -78.2 | -0.7 | $a$ |
|  | 72.5 | 79 | -6.5 | j | $\mathrm{CH}_{3} \mathrm{COCH}_{2} \mathrm{COCH}_{3}$ | -83.3 | -90.5 | +7.2 | $a$ |
| $\mathrm{HN}_{3}$ | 73.0 | 70.3 | -6.5 +2.7 | h | $\bigcirc=0$ | -33.1 | -29.3 | -3.8 | $a$ |
|  | 73.0 | 70.3 | +2.7 | $h$ $k$ |  |  |  |  |  |
| $\mathrm{O}_{2}$ $\mathrm{O}_{3}$ | 12.2 48.5 | 22.0 34.2 | -9.8 14.3 | k.l |  | -9.8 | -8.8 | $-1.0$ | $a$ |
| $\mathrm{H}_{2} \mathrm{O}$ | -60.9 | -57.8 | 14.3 -3.1 | g g |  |  |  |  |  |
| $\mathrm{CH}_{3} \mathrm{OH}$ | -57.4 | -48.1 | -9.3 | $a$ | $\stackrel{\mathrm{CH}}{2} \mathrm{COOH}$ | -92.7 -101.2 | -90.6 -103.3 | -2.1 +2.1 | $a$ |
| $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$ | -63.0 | -56.2 | -6.8 | $a$ | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{COOH}$ | -105.7 | -108.4 | +2.7 | $a$ |
| $n \cdot \mathrm{C}_{3} \mathrm{H}_{7} \mathrm{OH}$ | -67.7 | -61.2 | -6.5 | $a$ | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{COOH}$ $(\mathrm{COOH})_{2}$ | -174.3 | -108.4 | +0.7 | $a$ |
| $i$ - $\mathrm{C}_{3} \mathrm{H}_{7} \mathrm{OH}$ | -65.4 | -65.1 | -0.3 | $a$ | - | -65.9 | -70.1 | + 2 | a |
| $t-\mathrm{C}_{4} \mathrm{H}_{9} \mathrm{OH}$ | -64.3 | -74.7 | +10.4 | $a$ |  |  |  | +4.2 | $a$ |
| $\mathrm{CH}_{3} \mathrm{OCH}_{3}$ | -51.2 | -44.0 | -7.2 | $a$ | $\bigcirc$ |  |  |  |  |
| $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OC}_{2} \mathrm{H}_{5}$ | -62.0 | -60.3 | -1.7 | $a$ | $\begin{aligned} & \mathrm{HCOOCH}_{3} \\ & \mathrm{CH}_{3} \mathrm{COOCH}_{3} \\ & \mathrm{CH}_{3} \mathrm{CO}-\mathrm{O}-\mathrm{COCH}_{3} \end{aligned}$ | -85.6 | -83.6 | -2.0 | $b$ |
| Do | -15.5 | -12.6 | -2.9 | $a$ |  | -93.6 -132.8 | -97.9 -137.1 | +4.3 +4.3 | $b$ |
|  |  | -12.6 | 2.9 | $a$ | $\mathrm{CH}_{3} \mathrm{CO}-\mathrm{O}-\mathrm{COCH}_{3}$ | -132.8 | -137.1 | +4.3 | $a$ |
| $\square 0$ | $-8.7$ | -8.3 | -0.4 | $a$ | 0 | -88.7 | -95.2 | +6.5 | $a$ |
| $\bigcirc-\mathrm{OH}$ | -24.7 | -23.0 | -1.7 | $a$ | 11 |  |  |  |  |
|  | -18.0 | -17.3 | -0.7 | $a$ | $\mathrm{HCONH}_{2}$ | -39.8 | -44.5 | +4.7 | $g$ |
| $\mathrm{HO}-\mathrm{OH}$ | -38.2 | -32.5 | -5.7 | $g$ | $\mathrm{HCON}\left(\mathrm{CH}_{3}\right)_{2}$ | -36.9 | -45.8 | +8.9 | $a$ |
| $\mathrm{CH}_{3} \mathrm{O}-\mathrm{OCH}_{3}$ | -28.3 | -30.1 | +1.8 | a | $\mathrm{N}_{2} \mathrm{O}$ | 30.9 | 19.6 | +11.3 | $g$ |
| $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{O}-\mathrm{OC}_{2} \mathrm{H}_{5}$ | -39.1 | -46.1 | +7.0 | $a$ | 0 | -40.6 | -18.8 | -21.8 | $g$ |
| CO | -6.2 | -26.4 | +20.2 | $a$ |  |  |  |  |  |
| $\mathrm{CO}_{2}$ | -75.4 | -94.1 | +18.7 | $a$ | $\mathrm{HONO}_{2}$ | -17.5 | -32.1 | +14.6 | $g$ |
| $\mathrm{C}_{3} \mathrm{O}_{2}$ | -24.1 | -22.4 | -1.7 | $a$ | $\mathrm{CH}_{3} \mathrm{ONO}$ | -36.6 | -15.8 | -20.8 | $a$ |
| $\mathrm{CH}_{2} \mathrm{O}$ | -33.0 | -26.0 | -7.0 | $a$ | $\mathrm{CH}_{3} \mathrm{NO}_{2}$ | 3.3 | -17.9 | +21.2 | $a$ |
| $\mathrm{CH}_{3} \mathrm{CHO}$ | -42.4 | -39.7 | -2.7 | $a$ |  |  |  |  |  |

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Table III. Heats of Isomerization $\Delta H_{\text {isom }}$ for Closed Shell Molecules

| Isomerization reaction | $\Delta H_{\text {isom }}, \mathrm{kcal} / \mathrm{mol}$ |  |  | Isomerization reaction | $\Delta H_{\text {isom }}, \mathrm{kcal} / \mathrm{mol}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Calcd | Exptl ${ }^{\text {a }}$ | Error |  | Calcd | Exptla | Error |
| $\mathrm{CH}_{3} \mathrm{C}=\mathrm{CH} \longrightarrow \mathrm{CH}_{2} \Longrightarrow \mathrm{C}=\mathrm{CH}_{2}$ | 2.9 | 1.3 | +1.6 | $\wedge \rightarrow+$ | 9.8 | -5.2 | +15.0 |
| $\mathrm{CH}_{3} \mathrm{C}=\mathrm{CH} \longrightarrow \mathrm{D}$ | 26.3 | 21.8 | +4.5 | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NH}_{2} \longrightarrow\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH}$ | 6.3 | 7.0 | -0.7 |
| $\mathrm{CH}_{3} \mathrm{CH}=\mathrm{CH}_{2} \rightarrow D$ | 6.3 | 7.8 | -1.5 |  | 1.8 | $>0^{c}$ |  |
| $\wedge$ trans $\rightarrow$ gauche | 0.5 | $0.6{ }^{\text {b }}$ | -0.1 | $\mathrm{CH}_{3} \mathrm{CN} \rightarrow \mathrm{CH}_{3} \mathrm{NC}$ | 41.1 | 14.7 | +26.4 |
| $\wedge \rightarrow \sim$ | 1.1 | 1.1 | 0.0 | $\stackrel{O}{\circ} \rightarrow{ }^{\circ}$ | 30.5 |  |  |
| $\mathbb{N} \rightarrow$ | 5.4 | 2.8 | +2.6 | $\bigcirc \mathrm{O} \rightarrow 0-0$ | 30.5 |  |  |
| $\mathbb{N} \rightarrow$ | 3.0 | -1.3 | +4.3 | $\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{OH} \longrightarrow\left(\mathrm{CH}_{3}\right)_{2} \mathrm{O}$ $\mathrm{CH}_{4} \mathrm{CH}=\mathrm{O} \longrightarrow \mathrm{CH}_{2}=\mathrm{CH}-\mathrm{OH}$ | $\begin{array}{r} 11.8 \\ 7.5 \end{array}$ | 12.2 | -0.4 |
|  | 0.5 | 2.0 | $-1.5$ | $\mathrm{CH}_{3} \mathrm{CH}=\mathrm{O} \rightarrow \mathrm{C}$ | 26.9 | 27.1 | -0.2 |
| 㒳 | 1.3 | 1.0 | +0.3 | $\mathrm{CH}_{3} \mathrm{COOH} \longrightarrow \mathrm{HCOOCH}_{3}$ | 15.6 | 19.7 | -4.1 |
| M $\rightarrow$ N | 7.2 | 7.2 | 0.0 |  | 1.6 | 0.5 | -1.1 |

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Table IV. Rotational Barriers

| Molecule | Barrier, kcal/mol |  |  | Ref |
| :---: | :---: | :---: | :---: | :---: |
|  | Calcd | Exptl | Error |  |
| $\mathrm{CH}_{2}=\mathrm{CH}_{2}$ | $62.5{ }^{\text {b }}$ | 65.0 | -2.5 | $a$ |
| $\mathrm{CH}_{3}-\mathrm{CH}_{3}$ | 1.0 | 2.9 | -1.9 | c |
| $\mathrm{CH}_{3}-\mathrm{NH}_{2}$ | 1.1 | 2.0 | -0.9 | $d$ |
| $\mathrm{CH}_{3}-\mathrm{OH}$ | 0.7 | 1.1 | -0.4 | $e$ |
| $\mathrm{NH}_{2}-\mathrm{NH}_{2}$ |  |  |  |  |
| Cis | 8.0 |  |  | $f$ |
| Trans | 0.0 |  |  |  |
| $\mathrm{HO}-\mathrm{OH}$ |  |  |  |  |
| Cis | 6.9 | 7.0 | -0.1 | $g$ |
| Trans | 0.0 | 1.1 | -1.1 |  |

${ }^{a}$ B. S. Rabinovitch and F. S. Looney, J. Chem. Phys., 23, 2439 (1965). ${ }^{b}$ Calculated without CI. ${ }^{c}$ S. Weiss and G. E. Leroi, J. Chem. Phys., 48, 962 (1968). ${ }^{d}$ D. R. Lide, Jr., ibid., 27, 343 (1957). ${ }^{e}$ E. V. Ivash and D. M. Dennison, ibid.. 21, 1804 (1953). ${ }^{f}$ No experimental data. Since the two a mino groups are orthogonal to each other in the equilibrium structure, there must be a finite trans barrier. $g$ R. H. Hunt, R. A. Leacock, C. W. Peters, and K. T. Hecht, J. Chem. Phys., 42, 1931 (1965).

Table V. Heats of Formation $\Delta H_{\mathrm{f}}$ for Neutral Radicals

| Radical | $\Delta H_{\mathrm{f}}, \mathrm{kcal} / \mathrm{mol}$ |  |  | Ref |
| :---: | :---: | :---: | :---: | :---: |
|  | Calcd | Exptl | Error |  |
| $\mathrm{CH}_{3}$ | 25.8 | 34.8 | -9.0 | $a$ |
| $\mathrm{CH}_{3} \mathrm{CH}_{2}$ | 12.8 | 25 | -12 | $b$ |
| $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}$ | 1.5 | 16.8 | -15.3 | $b$ |
| $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{C}$ | -7.2 | 4.5 | -11.7 | $b$ |
| Vinyl | 63.7 | 59.6 | +4.1 | $c$ |
| Allyl | 35.3 | 40 | -5 | c |
| $\mathrm{NH}_{2}$ | 37.1 | 40.1 | -3.0 | $a$ |
| $\mathrm{CH}_{3} \mathrm{NH}$ | 32.9 | 37 | -4 | $b$ |
| OH | 0.5 | 9.5 | -9.0 | d |
| $\mathrm{CH}_{3} \mathrm{O}$ | 0.1 | -0.5 | +0.6 | $b$ |
| HCO | -0.5 | 10.4 | -10.9 | d |
| NO | -0.2 | 21.6 | -21.8 | $a$ |
| $\mathrm{NO}_{2}$ | -4.6 | 7.9 | -12.5 | $a$ |
| $\mathrm{N}_{3}$ | 102.4 | 99 | +3 | $d$ |

" See footnote $g$ of Table II. ${ }^{b}$ J. L. Franklin, J. G. Dillard, H. M. Rosenstock, J. T. Herron, K. Draxl, and F. H. Field, Natl. Stand. Ref. Data Ser.. Natl, Bur. Stand.. No. 26 (1969). ${ }^{\text {c F. P. Lossing, Can. J. }}$ Chem., 49, 357 (1971). ${ }^{d}$ M. W. Chase, J. L. Curnutt, A. T. Hu, H. Prophet, A. N. Syverud, and L. C. Walker, J. Phys. Chem. Ref. Data, 3,311(1974).

MNDO approximations since they appeared throughout during our parametrization studies for every combination of parametric functions investigated. ${ }^{1}$ As for the third shortcoming (NO bonds), it should be remembered that no molecules with NO bonds were used during the parametrization. ${ }^{1}$ It is possible that the errors might have been reduced by a reparametrization, including such compounds in the basis set. Since, however, there was no guarantee that this would be the case and since the errors were not at all excessive, we did not feel that the considerable cost of the reparametrization would be justified.

Even in these three areas the errors in the MNDO heats of formation remain within bounds. The only compound for which the MNDO error exceeds $25 \mathrm{kcal} / \mathrm{mol}$ is cubane (error, -49.6 $\mathrm{kcal} / \mathrm{mol}$ ), a compound containing six fused four-membered rings. It is amusing to note that MINDO/ 3 gave a much better result in this case (error, $-8.9 \mathrm{kcal} / \mathrm{mol}^{2}$ ). Since cubane is a "globular" molecule, and since MINDO/3 gives heats of formation that are too positive in such cases, this tendency

Table VI. Heats of Formation $\Delta H_{\mathrm{f}}$ for Cations

| Cation | , $\Delta H_{\mathrm{f}}, \mathrm{kcal} / \mathrm{mol}$ |  |  | Ref |
| :---: | :---: | :---: | :---: | :---: |
|  | Calcd | Exptl | Error |  |
| $\mathrm{CH}_{3}{ }^{+}$ | 243.9 | 260 | -16 | $a$ |
| $\mathrm{CH}_{3} \mathrm{CH}_{2}{ }^{+}$ | 219.7 h | 219 | +1 | $b$ |
| $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}^{+}$ | 200.8 | 192 | +9 | $c$ |
| $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{C}^{+}$ | 187.3 | 176 | +11 | $b$ |
| $\mathrm{CH}_{2}=\mathrm{CH}^{+}$ | $265.5{ }^{h}$ | 266 | 0 | d |
| $\widehat{\sim}$ | 221.3 | 226 | -5 | d |
| $\oplus$ | 207.5 | 209 | -1 | $b$ |
| (О)- ${ }^{+} \mathrm{H}_{2}$ | 217.9 | 216 | +2 | $b$ |
| $\mathrm{NH}_{4}{ }^{+}$ | 165.0 | 155 | +10 | $e$ |
| $\mathrm{CH}_{2}=\mathrm{NH}_{2}{ }^{+}$ | 186.9 | 178 | +9 | $b$ |
| $\mathrm{H}_{3} \mathrm{O}^{+}$ | 134.2 | 139 | -5 | $f$ |
| $\mathrm{HCO}^{+}$ | 184.6 | 199 | -14 | $a$ |
| $\mathrm{CH}_{2}=\mathrm{O}^{+} \mathrm{H}$ | 155.5 | 167 | -11 | f |
| $\mathrm{NO}^{+} \mathrm{NO}^{+}$ | 230.5 240.5 | 237 | -6 +8 | $f$ |
| $\mathrm{NO}_{2}{ }^{+}$ | 240.5 | 233 | $+8$ | $b$ |

$a_{\text {See footnote } d}$ of Table V. $b$ See footnote $b$ of Table V. $c$ S. L. Chong and J. L. Franklin, J. Am. Chem. Soc., 94, 6347 (1972). ${ }^{d}$ See footnote $c$ of Table V. ${ }^{e}$ P. Kebarle, R. Tamdagni, H. Kirooka, and T. B. McMahon, Int. J. Mass Spectrom. Ion Phys., 19, 71 (1976). $f$ See footnote $g$ of Table II. $g$ J. Vogt and J. L. Beauchamp, J. Am. Chem. Soc., 97, 6682 (1975). ${ }^{h}$ Value for the classical cation which is predicted to be more stable than the nonclassical one.

Table VII. Mean Absolute Errors for Optimized Bond Lengths and Bond Angles ${ }^{a}$

| Geometrical variable | No. | Mean absolute error |  |
| :---: | :---: | :---: | :---: |
|  |  | MNDO | MINDO/3 |
| All bond lengths, $\AA$ | 228 | 0.014 | 0.022 |
| $\rightarrow \mathrm{C}-\mathrm{H}, \AA$ | 25 | 0.012 | 0.017 |
| $=\mathrm{C}-\mathrm{H}, \mathrm{A}$ | 25 | 0.006 | 0.021 |
| $\equiv \mathrm{C}-\mathrm{H}, \mathrm{A}$ | 6 | 0.006 | 0.019 |
| All CH, $\AA$ | 56 | 0.009 | 0.019 |
| $\mathrm{C}-\mathrm{C}, \AA$ | 58 | 0.012 | 0.019 |
| $\mathrm{C}=\mathrm{C}, \AA$ | 31 | 0.012 | 0.014 |
| $\mathrm{C} \equiv \mathrm{C}, \AA$ | 7 | 0.009 | 0.002 |
| All CC, $\AA$ | 96 | 0.012 | 0.016 |
| NH, A | 9 | 0.006 | 0.019 |
| $\mathrm{N}-\mathrm{C}, \mathrm{A}$ | 8 | 0.008 | 0.051 |
| $\mathrm{N} \equiv \mathrm{C}, \mathrm{A}$ | 6 | 0.008 | 0.004 |
| All NC, $\AA$ | 17 | 0.010 | 0.029 |
| NN, $\AA$ | 9 | 0.032 | 0.074 |
| $\mathrm{OH}, \AA$ | 7 | 0.011 | 0.010 |
| $\mathrm{O}-\mathrm{C}, \mathrm{A}$ | 8 | 0.016 | 0.047 |
| $\mathrm{O}=\mathrm{C}, \mathrm{A}$ | 14 | 0.017 | 0.012 |
| All OC, $\AA$ | 22 | 0.016 | 0.025 |
| ON, $\AA$ | 8 | 0.026 | 0.026 |
| OO, \& | 3 | 0.117 | 0.043 |
| All bond angles, ${ }^{b}$ deg | 91 | 2.8 | 5.6 |
| HCH , deg | 15 | 3.1 | 6.1 |
| HCC, deg | 23 | 1.3 | 2.6 |
| CCC, ${ }^{\text {d deg }}$ | 12 | 2.0 | 5.9 |
| All angles at $C,{ }^{\text {b }}$ deg | 62 | 2.0 | 4.4 |
| All angles at $\mathrm{N},{ }^{b}$ deg | 15 | 3.2 | 7.1 |
| All angles at $0, b$ deg | 9 | 8.5 | 10.7 |
| Angles between planes in bicyclic compounds, deg | 5 | 1.6 | 5.9 |

$a$ Based on the results in Table VIII. ${ }^{b}$ Bond angles in rings are not included since they are mainly determined by the topology of the ring. The errors for these angles are considerably smaller than those given in the table.
presumably balanced the equal tendency to give too negative heats of formation for compounds containing four-membered rings. In MNDO the former tendency is corrected, but not the latter, so the calculated heat of formation is much too negative.

Table VIll. Molecular Geometries

| Molecule | Point group | Calcd (obsd) values for geometrical variables ${ }^{\text {a }}$ | Ref |
| :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2}$ | $D_{\text {ch }}$ | HH 0.663 (0.742) | $b$ |
| $\mathrm{CH}_{4}$ | $T_{d}^{\text {a }}$ | CH 1.104 (1.094) | c |
| $\mathrm{C}_{2} \mathrm{H}_{6}$ | ${ }^{\text {d }}$ d | CC 1.521 (1.536), CH 1.109 (1.091), HCC 111.2 (110.9) | $c$ |
| $\mathrm{C}_{2} \mathrm{H}_{4}$ | $D_{2 h}$ | CC 1.335 (1.339), CH 1.089 (1.086), HCC 123.2 (121.2) | $c$ |
| $\mathrm{C}_{2} \mathrm{H}_{2}$ | $D_{\text {ah }}$ | CC 1.194 (1.203), CH 1.051 (1.060) | $c$ |
|  | $C_{2 v}$ | CC $1.530(1.526), \mathrm{C}^{\prime} \mathrm{H}^{4} 1.110(1.089), \mathrm{C}^{\prime} \mathrm{H}^{5} 1.109$ (1.094), $\mathrm{C}^{2} \mathrm{H}^{7} 1.115(1.096), \mathrm{C}^{1} \mathrm{C}^{2} \mathrm{C}^{3}$ 115.4 (112.4), $\mathrm{H}^{7} \mathrm{C}^{2} \mathrm{H}^{8} 106.0$ (106.1), $\mathrm{H}^{4} \mathrm{C}^{1} \mathrm{C}^{2} 110.3$ (111.8), $\mathrm{H}^{5} \mathrm{C}^{1} \mathrm{H}^{6} 107.9$ (107.3), $\mathrm{C}^{2}-\mathrm{C}^{1} \mathrm{H}^{5} \mathrm{H}^{6} 129.0$ (12.6.4) | $d$ |
|  | $c_{s}$ | $\begin{aligned} & \mathrm{C}^{1} \mathrm{C}^{2} 1.340(1.336), \mathrm{C}^{2} \mathrm{C}^{3} 1.496(1.501), \mathrm{C}^{1} \mathrm{H}^{4} 1.089(1.081), \mathrm{C}^{1} \mathrm{H}^{5} 1.089(1.091), \mathrm{C}^{2} \mathrm{H}^{6} \\ & 1.096(1.090), \mathrm{C}^{3} \mathrm{H}^{7} 1.109(1.085), \mathrm{C}^{3} \mathrm{H}^{8} 1.111(1.098), \mathrm{C}^{1} \mathrm{C}^{3} \mathrm{C}^{126.9}(124.3), \mathrm{H}^{4} \mathrm{C}^{1} \mathrm{C}^{8} \\ & 122.4(121.5), \mathrm{H}^{5} \mathrm{C}^{2} \mathrm{C}^{2} 124.3(120.5), \mathrm{H}^{6} \mathrm{C}^{2} \mathrm{C}^{1} 119.3(19.0), \mathrm{H}^{7} \mathrm{C}^{3} \mathrm{C}^{2} 113.1(111.2), \mathrm{H}^{8} \mathrm{C}^{3}{ }^{9} \\ & 107.7(106.2), \mathrm{C}^{2}-\mathrm{C}^{3} \mathrm{H}^{8} \mathrm{H}^{9} 126.1(126.0) \end{aligned}$ | $e$ |
| $\mathrm{CH} \equiv \mathrm{C}-\mathrm{CH}_{3}$ | $C_{3 v}$ | $\begin{aligned} & \mathrm{C}^{1} \mathrm{C}^{2} 1.196(1.206), \mathrm{C}^{2} \mathrm{C}^{3} 1.445(1.459), \mathrm{C}^{1} \mathrm{H} 1.050(1.056), \mathrm{C}^{3} \mathrm{H} 1.111 \text { (1.105), } \mathrm{C}^{2} \mathrm{C}^{3} \mathrm{H} 111.0 \\ & (110.2) \end{aligned}$ | $f$ |
| $\mathrm{CH}_{2}=\mathrm{C}=\mathrm{CH}_{2}$ | $\begin{aligned} & D_{2 d} \\ & C_{2} \end{aligned}$ | CC 1.306 (1.308), CH 1.090 (1.087), HCH 114.2 (118.2) <br> $\mathrm{C}^{\prime} \mathrm{C}^{2} 1.531$ (1.533), $\mathrm{C}^{2} \mathrm{C}^{3} 1.539$ (1.533), $\mathrm{C}^{1} \mathrm{C}^{2} \mathrm{C}^{3} 114.8$ (112.8) | $\begin{aligned} & g \\ & h \end{aligned}$ |
| $\rangle$ | $C_{3 v}$ | CC 1.541 (1.525), CCC 112.3 (111.2) | $i$ |
| $\mathbb{N}$ | $C_{2 h}$ | $\mathrm{C}^{1} \mathrm{C}^{2} 1.497$ (1.508), $\mathrm{C}^{2} \mathrm{C}^{3} 1.346$ (1.347), $\mathrm{C}^{1} \mathrm{C}^{2} \mathrm{C}^{3} 126.3$ (123.8) | j |
|  | $C_{2 v}$ | $\mathrm{C}^{1} \mathrm{C}^{2} 1.348$ (1.330), $\mathrm{C}^{2} \mathrm{C}^{3} 1.508$ (1.507), $\mathrm{C}^{1} \mathrm{C}^{2} \mathrm{C}^{3} 121.9$ (122.4) | $k$ |
| $\mathbb{N}$ | $C_{2 h}$ | $\mathrm{C}^{1} \mathrm{C}^{2} 1.344$ (1.341), $\mathrm{C}^{2} \mathrm{C}^{3} 1.465$ (1.463), $\mathrm{C}^{1} \mathrm{C}^{2} \mathrm{C}^{3} 125.7$ (123.3) | $l$ |
| $\begin{aligned} & \mathrm{CH}_{3} \mathrm{C} \equiv \mathrm{CCH}_{3} \\ & \mathrm{CH} \equiv \mathrm{C}-\mathrm{CH}=\mathrm{CH}_{2} \end{aligned}$ | $\begin{aligned} & D_{3 d} \\ & C_{S} \end{aligned}$ | $\begin{aligned} & \mathrm{C}^{1} \mathrm{C}^{2} 1.444(1.467), \mathrm{C}^{2} \mathrm{C}^{3} 1.199(1.213), \mathrm{C}^{1} \mathrm{H} 1.111(1.115), \mathrm{HC}^{1} \mathrm{C}^{2} 111.0(110.7) \\ & \mathrm{C}^{1} \mathrm{C}^{2} 1.198(1.208), \mathrm{C}^{2} \mathrm{C}^{3} 1.417(1.431), \mathrm{C}^{3} \mathrm{C}^{4} 1.345(1.341), \mathrm{C}^{2} \mathrm{C}^{3} \mathrm{C}^{4} 125.3(123.1) \end{aligned}$ | ${ }_{m}^{m}$ |
| $\mathrm{CH} \equiv \mathrm{C}-\mathrm{C}=\mathrm{CH}$ | $D_{\text {ch }}$ | $\mathrm{C}^{1} \mathrm{C}^{2} 1.199$ (1.205), $\mathrm{C}^{2} \mathrm{C}^{3} 1.368$ (1.376), $\mathrm{C}^{1} \mathrm{H} 1.051$ (1.046) ${ }^{\text {c }}$ |  |
| $\mathrm{CH}_{2}=\mathrm{C}=\mathrm{C}=\mathrm{CH}_{2}$ | $D_{2 h}$ | $\mathrm{C}^{1} \mathrm{C}^{2} 1.310$ (1.318), $\mathrm{C}^{2} \mathrm{C}^{3} 1.270$ (1.283), $\mathrm{C}^{1} \mathrm{H} 1.090$ (1.083) | o |
| $\mathrm{C}\left(\mathrm{CH}_{3}\right)_{4}$ | $T_{d}$ | CC 1.554 (1.539), CH 1.109 (1.120), HCC 111.7 (110.0) | $p$ |
| D | $D_{3 h}$ | CC 1.525 (1.510), CH 1.096 (1.089), HCH 110.8 (115.1) | 9 |
| D | $C_{2 v}$ | $\begin{aligned} & \mathrm{C}^{1} \mathrm{C}^{2} 1.328(1.296), \mathrm{C}^{2} \mathrm{C}^{3} 1.512(1.509), \mathrm{C}^{1} \mathrm{H} 1.062(1.072), \mathrm{C}^{3} \mathrm{H} 1.097(1.088), \mathrm{HC}^{1} \mathrm{C}^{2} \\ & \quad 151.6(149.9), \mathrm{HC}^{3} \mathrm{H} 111.0(114.6) \end{aligned}$ | $r$ |
| $\square$ | $D_{2 d}$ | CC 1.549 (1.548), CH 1.105 (1.133), HCH 107.6 (108.1), $\mathrm{C}^{1} \mathrm{C}^{2} \mathrm{C}^{4} \mathrm{C}^{3} 180.0$ (153.0). | $s$ |
| $\square$ | $C_{2 v}$ | $\begin{gathered} \mathrm{C}^{1} \mathrm{C}^{2} 1.355(1.342), \mathrm{C}^{2} \mathrm{C}^{3} 1.525(1.517), \mathrm{C}^{3} \mathrm{C}^{4} 1.568(1.566), \mathrm{C}^{3} \mathrm{H} 1.075(1.083), \mathrm{C}^{3} \mathrm{H} \\ \left.1.104(1.094), \mathrm{HC}^{1} \mathrm{C}^{2} 135.8(133.5), \mathrm{HC}^{3} \mathrm{H} 108.4(109.2), \mathrm{C}^{1}-\mathrm{C}^{4} \mathrm{H}_{2} 136.84135 .8\right) \end{gathered}$ | $t$ |
| ) | $C_{s}$ | CC 1.542 (1.546), CH 1.111 (1.114), HCC 110.7 (111.7) ${ }^{\text {(1) }}$ | $u, v$ |
|  | $C_{2 v}$ | $\mathrm{C}^{1} \mathrm{C}^{2} 1.362$ (1.342), $\mathrm{C}^{2} \mathrm{C}^{3} 1.477$ (1.469), $\mathrm{C}^{1} \mathrm{C}^{5} 1.521$ (1.509) | $w$ |
| $\square=$ | $C_{2 v}$ | $\mathrm{C}^{1} \mathrm{C}^{2} 1.491$ (1.470), $\mathrm{C}^{2} \mathrm{C}^{3} 1.366$ (1.355), $\mathrm{C}^{3} \mathrm{C}^{4} 1.477$ (1.476), $\mathrm{C}^{1} \mathrm{C}^{6} 1.345$ (1.349) | $x$ |
| $\square$ | $D_{3 d}$ | $\begin{aligned} & \text { CC } 1.539 \text { (1.536), CH } 1.114 \text { (1.121), CCC } 114.1 \text { (111.4), HCH } 105.7 \text { (107.5), CCCC } 46.3 \\ & (54.9) \end{aligned}$ | $y$ |
| $\square$ | $C_{2}$ | ```C'C}\mp@subsup{C}{}{2}1.346(1.335),\mp@subsup{C}{}{2}\mp@subsup{C}{}{3}1.504(1.504),\mp@subsup{C}{}{3}\mp@subsup{C}{}{4}1.541 (1.515), C4 C C 1.539 (1.550), C}\mp@subsup{C}{}{1}\mp@subsup{C}{}{2}\mp@subsup{\textrm{C}}{}{4}\mp@subsup{\textrm{C}}{}{5}21.8(28.3``` | $z$ |
| $\bigcirc$ | $D_{6} h$ | CC 1.407 (1.397), CH 1.090 (1.084) | $c$ |
| $N$ | $C_{2 v}$ | $\begin{aligned} & \mathrm{C}^{1} \mathrm{C}^{2} 1.526(1.498), \mathrm{C}^{1} \mathrm{C}^{3} 1.537(1.497), \mathrm{C}^{1} \mathrm{H} 1.074(1.071), \mathrm{C}^{2} \mathrm{H}_{\mathrm{eq}} 1.098(1.093), \mathrm{C}^{2} \mathrm{H}_{\mathrm{ax}} \\ & \quad 1.097(1.093), \mathrm{C}^{2} \mathrm{C}^{3} \mathrm{C}^{4} \mathrm{C}^{4} 122.7(121.7) \end{aligned}$ | a |
| $\infty$ | $D_{2 d}$ | $\begin{aligned} & \mathrm{C}^{1} \mathrm{C}^{2} 1.509(1.469), \mathrm{C}^{2} \mathrm{C}^{3} 1.529(1.519), \mathrm{C}^{2} \mathrm{H} 1.096(1.091), \mathrm{HC}^{2} \mathrm{H} 111.0(118.4), \mathrm{C}^{3}-\mathrm{C}^{2} \mathrm{H}_{2} \\ & 150.6(148.3) \end{aligned}$ | $b b$ |
|  | $C_{s}$ | $\begin{aligned} & C^{1} C^{2} 1.540(1.528), C^{2} C^{3} 1.563(1.565), C^{1} C^{4} 1.555(1.536), C^{1} C^{5} 1.530(1.507), C^{5} C^{4} C^{1} C^{2} \\ & 117.4(116.7) \end{aligned}$ | cc |
|  | $c_{s}$ | $\begin{aligned} & C^{1} C^{2} 1.524(1.511), C^{2} C^{3} 1.361(1.341), C^{1} C^{4} 1.567(1.543), C^{1} C^{5} 1.534(1.533), C^{5} C^{4} C^{1} C^{2} \\ & 117.6(114.5) \end{aligned}$ | $d d$ |
|  | $C_{2 v}$ | $\begin{aligned} & C^{1} C^{2} 1.561(1.539), C^{2} C^{3} 1.557(1.557), C^{1} C^{7} 1.562(1.560), C^{1} C^{7} C^{4} 93.2(93.1), \\ & C^{6} C^{1} C^{4} C^{3} 114.2(113.1) \end{aligned}$ | $e e$ |
|  | $C_{2 v}$ | ```C'C}\mp@subsup{C}{}{2}1.540(1.535),\mp@subsup{C}{}{2}\mp@subsup{C}{}{3}1.358(1.343),\mp@subsup{C}{}{1}\mp@subsup{C}{}{7}1.579 (1.573), C' C C C C 91.7 (94.1), C}\mp@subsup{}{}{6}\mp@subsup{\textrm{C}}{}{1}\mp@subsup{C}{}{4}\mp@subsup{\textrm{C}}{}{3}113.4 (115.6``` | $e e$ |
| $\bigcirc$ | $D_{2 h}$ | $\mathrm{C}^{1} \mathrm{C}^{2} 1.382$ (1.364), $\mathrm{C}^{2} \mathrm{C}^{3} 1.429$ (1.415), $\mathrm{C}^{1} \mathrm{C}^{9} 1.439$ (1.421), $\mathrm{C}^{9} \mathrm{C}^{10} 1.435$ (1.418) | ff |
| $\mathrm{N}_{2}$ | $D_{\text {mh }}$ | NN 1.103 (1.094) | $b$ |
| $\mathrm{NH}_{3}$ | $C_{3 v}$ | NH 1.007 (1.012), HNH 105.3 (106.7) | $c$ |
| $\mathrm{CH}_{3} \mathrm{NH}_{2}$ | $C_{s}$ | CN 1.460 (1.474), NH 1.008 (1.011), HNC 109.8 (112.0), HNH 105.6 (105.9) | $g g$ |


|  | Point |  |  |
| :--- | :--- | :--- | :--- | :--- |
| group |  |  |  |

[^0]Table VIII (Continued)
clockwise along $\mathrm{B}-\mathrm{C}$, and angle $\mathrm{A}^{i}-\mathrm{B}^{j} \mathrm{C}^{k} \mathrm{D}^{l}$ (in deg) of $\mathrm{A}-\mathrm{B}$ with the plane BCD . The superscripts $i, j, k, l$ number the atoms in the molecule according to IUPAC rules; they are left out when the atoms can be specified unambiguously without them. ${ }^{b}$ G. Herzberg, "Molecular Spectra and Molecular Structure I. Spectra of Diatomic Molecules", 2nd ed, Van Nostrand, New York, N.Y., 1950. ${ }^{\text {CG G. Herzberg, "Molecular Spectra }}$ and Molecular Structure III. Electronic Spectra and Electronic Structure of Polyatomic Molecules", Van Nostrand, New York, N.Y., 1966. ${ }^{d}$ D. R. Lide, Jr., J. Chem. Phys., 33, 1514 (1960). ${ }^{e}$ D. R. Lide, Jr., and D. Clristensen, ibid., 35, 1374 (1961). fC. C. Costain, ibid., 29,
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The relative energies of pairs of isomers are generally well reproduced by MNDO; see Table III. The only serious discrepancy occurs in the comparison $n$-pentane/neopentane, where MNDO predicts the latter to be much less stable. This of course is due to the tendency of MNDO to give heats of formation for crowded molecules that are too positive. The error here is, however, less than it was in MINDO/3 ( $\Delta H_{\text {isom }}$ (calcd), $24.5 \mathrm{kcal} / \mathrm{mol}$ ).

Rotational barriers (see Table IV) are predicted only moderately well by MNDO. As in MINDO/3, the calculated barrier for ethane is about one-third of the experimental value. For hydrazine and hydrogen peroxide, MNDO fails to reproduce the trans barriers, although the difference in energy between the trans and cis conformations is quite well reproduced. In the case of hydrogen peroxide, it is not surprising that no trans barrier is predicted since the inclusion of polarization functions in the basis set is found essential to obtain a barrier. ${ }^{4}$ For hydrazine, the MNDO torsional potential shows a shoulder at $90^{\circ}$ but no local minimum; we have to conclude that the tendency of the lone pairs to be orthogonal to each other (which is responsible for the skew structure of hydrazine ${ }^{5}$ ) is underestimated in MNDO.

Table V lists MNDO heats of formation for neutral radicals, calculated by the half-electron approximation, ${ }^{6,7}$ while Table VI gives MNDO heats of formation for some closed shell cations. The mean absolute errors for radicals ( $8.7 \mathrm{kcal} / \mathrm{mol}$ ) and for cations ( $7.2 \mathrm{kcal} / \mathrm{mol}$ ) are slightly higher than for neutral molecules ( $6.3 \mathrm{kcal} / \mathrm{mol}$ ) but of the same order of magnitude. The radicals systematically tend to be predicted somewhat too stable, whereas there is no such trend for the cations.

## (III) Molecular Geometries

Table VII compares MNDO and MINDO/3 results for bond lengths and bond angles. Table VIII shows the optimized MNDO structures for 80 molecules, along with the experimental data. Full structures are given for small molecules, but as a rule only the molecular skeletons are given for larger ones. When comparing calculated and observed values for geometrical variables, it should be remembered that the experimental $r_{\mathrm{s}}$ values from microwave spectroscopy and $r_{\mathrm{g}}$ values from electron diffraction differ somewhat from the equilibrium $r_{e}$ values. Discrepancies of less than $0.01 \AA$ in bond lengths and $1^{\circ}$ in angles are therefore not too meaningful.

The mean absolute error in bond lengths (see Table VII) is reduced from $0.022 \AA$ in MINDO $/ 3$ to $0.014 \AA$ in MNDO. Major improvements are found for $\mathrm{CH}, \mathrm{NH}, \mathrm{NN}, \mathrm{N}-\mathrm{C}$, and $\mathrm{O}-\mathrm{C}$ bonds, whereas MINDO/3 is superior for OO bond lengths, for which the MNDO values are much too small. This failure of MNDO is related to the use of atomic parameters.

Table IX. Mean Absolute Errors $\Delta I P_{1}$ for First Ionization Potentials ${ }^{a}$

|  |  | $\Delta \mathrm{IP}, \mathrm{eV}$ |  |
| :--- | :---: | :--- | :---: |
| Class of compd | No. | MNDO | MINDO/3 |
| All compounds | 51 | 0.48 | 0.71 |
| Hydrocarbons | 22 | 0.41 | 0.31 |
| Nitrogen compounds (CHN) | 13 | 0.54 | 1.58 |
| Oxygen compounds (CHO) | 16 | 0.53 | 0.56 |

${ }^{a}$ Based on the results in Table $\mathbf{X}$.

Table X. First Ionization Potentials IP

${ }^{a}$ Calculated via Koopmans' theorem. $b$ Vertical ionization potentials from UV-photoelectron spectroscopy. $c \mathrm{D}$. W. Turner, C. Baker, A. D. Baker, and C. R. Brundle, "Molecular Photoelectron Spectroscopy", Wiley-Interscience, London, 1970. d Band center (average of Jahn-Teller peaks). ${ }^{e}$ J. N. Murrell and W. Schmidt, J. Chem. Soc. Faraday Trans. 2, 68, 1709 (1972). f. A. Katrib and J. W. Rabalais, J. Phys. Chem., 77, 2358 (1973). gF. Brogli, J. K. Crandall, E. Heilbronner, E. Kloster-Jensen, and S. A. Sojka, J. Electron Spectrosc. Relat. Phenom. 2,455 (1973). hP. Bischof and E. Heilbronner, Helr. Chim. Acta, 53, 1677 (1970). iP. Bischof, E. Haselbach, and E. Heilbronner, Angew, Chem., Int. Ed. Engl. 9, 953 (1970). JP. J. Derrick, L. Åsbrink, O. Edquist, B. O. Jonsson, and E. Lindholm, J. Mass. Spectrom. Ion Phys., 6, 161, 177, 191, 203 (1971). $k$ J. P. Maier and D. W. Turner, J. Chem. Soc., Faraday Trans. 2, 69, 521 (1973). ${ }^{l}$ See ref 11 b. $m$ R. F. Lake and H. Thompson, Proc. R. Soc. London, Ser. A, 317, 187 (1970). nC. R. Brundle, Chem. Phys. Lett., 26, 25 (1974). OM. B. Robin and N. A. Kuebler, J. Electron Spectrosc. Relat. Phenom., 1, 13 (1972). p S. Cradock and R. A. Whiteford, J. Chem. Soc., Faraday Trans. $2,68,281$ (1972). $q$ W. C. Tam, D. Yee, and C. E. Brion, J. Electron Spectrosc. Relat. Phenom., 4, 77 (1974). rC. R. Brundle, M. B. Robin, N. A. Kuebler, and H. Basch, J. Am. Chem. Soc., 94, 1451 (1972). sC. R. Brundle, D. W. Turner, M. B. Robin, and N. A. Kuebler, Chem. Phys. Lett. 3, 292 (1969). tD. A. Sweigart and D. W. Turner. J. Am. Chem. Soc. 94, 5592 (1972).

When bond parameters were used in our MNDO parametrization studies, ${ }^{1}$ the OO bond lengths could be reproduced without difficulty.

The mean absolute error in bond angles (see Table VII) is reduced from $5.6^{\circ}$ in MINDO $/ 3$ to $2.8^{\circ}$ in MNDO. HCH angles, CCC angles in acyclic compounds, angles at nitrogen, and flap angles in $\mathrm{b}^{\text {; yyclic compounds are all predicted more }}$ reliably in MNDO trian in MINDO/3. Bond angles at oxygen tend to be too large in MNDO and HCH angles slightly too small, although the errors are decreased compared to MINDO/3.

Ring conformations are not reproduced well by either MNDO or MINDO/3. Both methods predict cyclobutane, cyclopentane, and cyclopentene to be essentially planar. Note that ab initio calculations with minimal basis sets also underestimate the puckering in these molecules. ${ }^{8}$ Cyclohexane and cyclohexene are predicted to be nonplanar, but the optimized structures are somewhat too flat. MNDO gives stronger puckering than MINDO/3.

Structures of trivalent nitrogen compounds are usually reproduced better by MNDO than by MINDO/3. Dimethylamine, trimethylamine, aniline, cyanamide, and nitramide are pyramidal in MNDO, mostly with structures close to experi-
ment, whereas they are planar, or almost planar, in MINDO/3.

## (IV) Ionization Potentials

Calculated and observed ionization potentials are compared in Tables IX-XI. The calculated values are negative orbital energies, i.e., we assume the validity of Koopmans' theorem ${ }^{9}$ which neglects the electronic reorganization and the change in correlation energy upon ionization. Apart from a few exceptions, the errors introduced by this approximation (Koopmans' defect ${ }^{10}$ ) are usually less than 1 eV .

The mean absolute error for the first ionization potential (see Table IX) is reduced from 0.71 eV in MINDO $/ 3$ to 0.48 eV in MNDO. The main improvement is for nitrogen-containing compounds. The first ionization potentials in MNDO tend to be slightly larger than the experimental values (see Table X ).

For higher ionization potentials (see Table XI), MNDO is clearly superior to MINDO/3. The ordering of the MNDO levels and their splittings agree very satisfactorily with experimental data. The results for $\mathbf{N}_{2}$ are particularly satisfying because the Hartree-Fock method fails to predict the ionizations even in the right order. ${ }^{12}$ The results for unsaturated

Table XI. Higher Ionization Potentials IP

| Molecule | IP, eV |  | Assignment ${ }^{\text {c }}$ | Ref |
| :---: | :---: | :---: | :---: | :---: |
|  | Calcd ${ }^{\text {a }}$ | Exptl ${ }^{\text {b }}$ |  |  |
| $\mathrm{CH}_{4}$ | 13.87 | $14.0{ }^{\text {d }}$ | $1 \mathrm{t}_{2}$ | $e$ |
|  | 30.61 | 22.91 | $1 a_{1}$ |  |
| $\mathrm{C}_{2} \mathrm{H}_{6}$ | 12.70 | 12.1 | $1 \mathrm{e}_{\mathrm{g}}$ | $f$ |
|  | 13.33 |  | $2 \mathrm{a}_{1 \mathrm{~g}}$ |  |
|  | 15.09 | 15.0 | $1 \mathrm{e}_{\mathrm{u}}$ |  |
|  | 24.81 | 20.41 | $1 \mathrm{a}_{2 \mathrm{u}}$ |  |
| $\mathrm{C}_{2} \mathrm{H}_{4}$ | 10.18 | 10.51 | $1 b_{1 u}$ | $g$ |
|  | 12.64 | 12.85 | $1 \mathrm{~b}_{1 \mathrm{~g}}$ |  |
|  | 14.61 | 14.66 | $2 \mathrm{a}_{\mathrm{g}}$ |  |
|  | 15.83 | 15.87 | $1 \mathrm{~b}_{2 \mathrm{u}}$ |  |
| $\mathrm{C}_{2} \mathrm{H}_{2}$ | 11.03 | 11.40 | $1 \pi_{u}$ | $f$ |
|  | 15.87 | 16.36 | $2 \sigma_{g}$ |  |
|  | 21.01 | 18.69 | $10_{u}$ |  |
|  | 9.39 | 9.24 | ${ }_{12} \mathrm{lg}_{\mathrm{g}}$ | $h$ |
| - | 12.48 | 11.49 | ${ }^{2} \mathrm{e}_{2 \mathrm{~g}}$ |  |
|  | 12.61 | 12.3 | $1{ }^{2} \mathrm{ar}$ |  |
|  | 14.45 | 13.8 | $2 \mathrm{e}_{1 \mathrm{u}}$ |  |
|  | 15.21 | 14.7 | $1 \mathrm{~b}_{2 \mathrm{u}}$ |  |
|  | 16.79 | 15.4 | $1 \mathrm{~b}_{1 u}$ |  |
|  | 17.53 | 16.85 | $2 \mathrm{a}_{1 \mathrm{~g}}$ |  |
| $\mathrm{NH}_{3}$ | 11.19 | 10.88 | $2 a_{1}{ }^{\text {a }}$ | $e$ |
|  | 16.73 | 16.0 | 1 e |  |
|  | 32.98 | 27.0 | $1 a_{1}$ |  |
| HCN | 13.42 | 13.60 | $1 \pi$ | $f$ |
|  | 14.26 | 14.0 | $3 \sigma$ |  |
|  | 21.63 | 19.95 | $2 \sigma$ |  |
| $\mathrm{N}_{2}$ | 14.88 | 15.60 | $2 \sigma_{\mathrm{g}}$ | $f$ |
|  | 16.22 | 16.98 | $1 \pi_{u}$ |  |
|  | 21.06 | 18.78 | $1 \sigma_{u}$ |  |
| $\mathrm{H}_{2} \mathrm{O}$ | 12.19 | 12.62 | $1 \mathrm{~b}_{1}$ | $e$ |
|  | 14.47 | 14.74 | $2 a_{1}$ |  |
|  | 19.11 | 18.51 | $1 \mathrm{~b}_{2}$ |  |
|  | 40.04 | 32.2 | $1 a_{1}$ |  |
| $\mathrm{CO}_{2}$ | 12.79 | 13.78 | $1 \pi \mathrm{~g}$ | $f$ |
|  | 17.69 | 17.59 | $1 \pi_{u}$ |  |
|  | 17.81 | 18.08 | $2 \sigma_{u}$ |  |
|  | 21.25 | 19.40 | $2 \sigma_{\mathrm{g}}$ |  |
| $\mathrm{CH}_{2}=\mathrm{O}$ | 11.04 | 10.88 | $2 b^{\text {b }}$ | $i$ |
|  | 14.19 | 14.38 | $1 \mathrm{~b}_{1}$ |  |
|  | 16.30 | 16.00 | 2 a, |  |
|  | 16.96 | 16.78 | $1 \mathrm{~b}_{2}$ |  |

${ }^{a}$ Calculated via Koopmans' theorem. ${ }^{b}$ Vertical ionization potentials from UV-photoelectron spectroscopy. ${ }^{c}$ The numbering of the MO's refers to a valence basis set. The assignments are taken from the references; MNDO gives identical assignments, in all cases. ${ }^{d}$ Band center (average of Jaln-Teller peaks). ${ }^{e}$ A. W. Potts and W. C. Price, Proc. R. Soc. London, Ser. A, 326, 165, 181 (1972). f See footnote $c$ of Table X. $g$ See footnote $r$ of Table X. ${ }^{h}$ See ref $1 \mathrm{lb} .{ }^{i} \mathrm{~A}$. D. Baker, C. Baker, C. R. Brundle, and D. W. Turner, J. Mass Spectrom. Ion Phys.. 1, 285 (1968). New experimental results show that the original assignment $\left(1 b_{2}, 2 a_{i}\right)$ of the last two bands has to be reversed, see: S. T. Hood, A. Hamnett, and C. E. Brion, Chem. Phys. Lett., 41, 428 (1976).
systems are also very satisfactory, all the ionizations being predicted in the order observed. Previous semiempirical treatments, including MINDO/3, had given spurious highlying $\sigma$ levels. Thus MNDO predicts the four highest levels of naphthalene to be of $\pi$ type, in agreement with ab initio calculations ${ }^{11 a}$ and experiment, ${ }^{11 b}$ whereas MINDO/3 inserted several $\sigma$ levels between the four highest $\pi$ MO's. The only shortcoming of MNDO is an overestimation of the ionization energies corresponding to MO's with high 2 s coefficients, e.g., $1 \mathrm{a}_{1}$ in methane, ammonia, or water. This is undoubtedly due to the neglect of $1 \mathrm{~s}-2 \mathrm{~s}$ interactions, arising from the use of the core approximation in MNDO. Such interactions will of course have little effect on the total energies of molecules but will affect the orbital energies of MO's derived largely from 2 s AO's.

Table XII. Mean Absolute Errors $\Delta \mu$ for Dipole Moments ${ }^{a}$

|  |  | $\Delta \mu, \mathrm{D}$ |  |
| :--- | ---: | :---: | :---: |
| Class of compd | No. | MNDO | MINDO/3 |
| All compounds | 57 | 0.30 | 0.49 |
| Hydrocarbons | 11 | 0.25 | 0.26 |
| Nitrogen compounds (CHN) | 18 | 0.41 | 0.77 |
| Oxygen compounds (CHO) | 22 | 0.19 | 0.37 |
| Nitrogen-oxygen compounds | 6 | 0.50 | 0.49 |

${ }^{a}$ Based on the results in Table XIII.

## (V) Dipole Moments and Charge Distributions

Calculated and observed dipole moments are compared in Tables XII and XIII. The mean absolute error for the dipole moments (Table XII) is reduced from 0.49 D in MINDO/3 to 0.30 D in MNDO. The greatest improvements are for systems containing heteroatoms. Dipole moments for unsaturated hydrocarbons are usually predicted too low in MNDO (Table XIII).

Net atomic charges for some simple molecules are listed in Table XIV. The MNDO values are usually similar to the corresponding STO-3G ones, ${ }^{13}$ which were calculated using orbital exponents optimized for each molecule. In heterosystems particularly, the charge separation between the carbon and hetero atoms is comparable for MNDO and STO-3G but much larger for MINDO/3. There are, however, a few significant differences.

In saturated hydrocarbons, MNDO yields the polarity $\mathrm{C}^{+}-\mathrm{H}^{-}$for the $\mathrm{C}-\mathrm{H}$ bond ${ }^{14}$ and STO-3G C-- $\mathrm{H}^{+}$, but the net charges are in both cases small. Substitution of a methyl group for a hydrogen atom at a center X makes the net atomic charge of X slightly more negative in MNDO but more positive in STO-3G (cf. the series $\mathrm{H}_{2} \mathrm{O}, \mathrm{CH}_{3} \mathrm{OH},\left(\mathrm{CH}_{3}\right)_{2} \mathrm{O}$ ). Again, the effects are small, but of opposite sign. Finally, MNDO seems to underestimate the polarization of $\pi$ electrons by alkyl substituents, judging by the low values of the dipole moments calculated for unsaturated hydrocarbons.

## (VI) Computational Aspects

Table XV lists the computation times required for one SCF calculation using various SCF methods. That for a MNDO calculation is only about $20 \%$ greater than for a MINDO/3 one. The rate-determining step in both cases is matrix diagonalization, not integral evaluation as in ab initio methods. Derivatives of the energy can therefore be calculated very rapidly in MNDO by finite difference, allowing the use of rapid and efficient procedures for locating minima and transition states on the potential surface for a reaction. The time required for such calculations is also only a little greater than it is for MINDO/3. ${ }^{15}$

Compared with STO-3G, a single SCF calculation with MNDO is faster "only" by a factor of about 20 (see Table XV). Since, however, the calculation of gradients in ab initio procedures is much more time consuming, geometry optimizations will be much faster in MNDO than in STO-3G (estimated factor, $100: 1$ ). The computational advantages of MNDO would of course be still more conspicuous in comparisons with more sophisticated ab initio methods.

## (VII) Conclusions

The data and statistics provided in the previous chapters show that the MNDO values for heats of formation, molecular geometries, ionization potentials, and dipole moments are quite close to the experimental values. The MNDO results are superior to the MINDO/3 ones in most respects, particularly for nitrogen-containing compounds. Qualitative improvements

Table XIII. Dipole Moments $\mu$

| Molecule | $\mu, \mathrm{D}$ |  |  | Ref | Molecule | $\mu, \mathrm{D}$ |  |  | Ref |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Calcd. | Exptl | Error |  |  | Calcd. | Exptl | Error |  |
| $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | 0.00 | 0.08 | -0.08 | $a$ | $\mathrm{CH}_{3} \mathrm{NH}-\mathrm{NH}_{2}$ | 1.538 | 1.668 | -0.13 | $h$ |
| $\mathrm{CH}_{3} \mathrm{CH}=\mathrm{CH}_{2}$ | 0.04 | 0.37 | -0.33 | $a$ | $\mathrm{CH}_{2} \mathrm{~N}_{2}$ | 1.25 | 1.50 | -0.25 | $a$ |
| $\mathrm{CH}_{3} \mathrm{C} \equiv \mathrm{CH}$ | 0.12 | 0.78 | -0.66 | $a$ | N |  |  |  |  |
| D | 0.48 | 0.45 | +0.03 | $a$ | $\cdots$ | 1.55 | 1.59 | -0.04 | $a$ |
| $\square$ | 0.08 | 0.13 | -0.05 | $a$ | $\mathrm{CH}_{3} \mathrm{~N}_{3}$ | 1.63 | 2.17 | -0.54 | $a$ |
| $\square$ |  |  |  |  | $\mathrm{O}_{3}$ | 1.18 | 0.53 | +0.65 | $a$ |
| 1 | 0.05 | 0.20 | -0.15 | $a$ | $\mathrm{H}_{2} \mathrm{O}$ | 1.78 | 1.85 | -0.07 | $a$ |
|  |  |  |  |  | $\mathrm{CH}_{3} \mathrm{OH}$ | 1.48 | 1.70 | -0.22 | $a$ |
| $\theta$ | 0.18 | 0.42 | -0.24 | $a$ | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$ | 1.40 | 1.69 | -0.29 | $a$ |
| $\bigcirc$ |  |  |  |  | $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{O}$ | 1.26 | 1.30 | -0.04 | $a$ |
|  | 0.22 | 0.62 | -0.40 | $b$ | $\left(\mathrm{C}_{2} \mathrm{H}_{5}\right)_{2} \mathrm{O}$ |  | 1.15 | -0.06 | $a$ |
|  |  |  |  |  | 10 |  |  |  | $a$ |
|  | 0.69 | 0.42 | +0.27 | $c$ | $\bigcirc-\mathrm{OH}$ | 1.67 | 1.45 | +0.22 | $a$ |
|  | 0.06 | 0.36 | -0.30 | $a$ | 0 | 0.42 | 0.66 | -0.24 | $a$ |
|  | 0.41 | 0.68 | -0.27 | $d$ |  | 1.44 | 1.38 | +0.06 | $a$ |
| $\mathrm{NH}_{3}$ | 1.76 | 1.47 | +0.29 | $a$ | CO | 0.19 | 0.11 | +0.08 | $a$ |
| $\mathrm{CH}_{3} \mathrm{NH}_{2}$ | 1.48 | 1.31 | +0.17 | $a$ | $\mathrm{CH}_{2} \mathrm{O}$ | 2.16 | 2.33 | -0.17 | $a$ |
| $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH}$ | 1.17 | 1.03 | +0.14 | $a$ | $\mathrm{CH}_{3} \mathrm{CHO}$ | 2.38 | 2.69 | -0.31 | $a$ |
| $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{~N}$ | 0.75 | 0.61 | +0.14 | $a$ | $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CO}$ | 2.51 | 2.88 | -0.37 | $a$ |
| $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NH}_{2}$ | 1.52 | 1.22 | $\div 0.30$ | $a$ | $\mathrm{CH}_{2} \mathrm{CO}$ | 1.04 | 1.42 | -0.38 | $a$ |
| LNH | 1.75 | 1.90 | -0.15 | $a$ | $\mathrm{CH}_{2}=\mathrm{CH}-\mathrm{CHO}$ | 2.93 | 3.12 | -0.19 +0.39 | $a$ |
|  |  |  |  |  | $\mathrm{CH}=\mathrm{C}-\mathrm{CHO}$ | 2.86 | 2.47 | +0.39 | $a$ |
| $\bigcirc \mathrm{NH}$ | 1.81 | 1.74 | $+0.07$ | $e$ | HCOOH | 1.49 | 1.41 | +0.08 | $a$ |
|  |  |  |  |  | $\mathrm{CH}_{3} \mathrm{COOH}$ | 1.68 | 1.74 | -0.06 | $a$ |
| $\mathrm{O}^{\mathrm{N}}$ | 1.97 | 2.22 | -0.25 | $f$ | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{COOH}$ | 1.64 | 1.75 | -0.11 | $a$ |
|  |  |  |  |  | $\mathrm{HCOOCH}_{3}$ | 1.63 | 1.77 | -0.14 | $a$ |
|  | 1.48 | 1.53 | -0.05 | $a$ | $\mathrm{CH}_{3} \mathrm{COOCH}_{3}$ | 1.74 | 1.72 | +0.02 | $a$ |
| HCN |  |  |  |  | $\mathrm{HCONH}_{2}$ | 3.09 | 3.73 | -0.64 | $a$ |
| $\mathrm{CH}_{3} \mathrm{CN}$ | 2.51 2.63 | 2.98 3.92 | -0.47 -1.29 | $a$ | $\mathrm{HCON}\left(\mathrm{CH}_{3}\right)_{2}$ | 3.19 | 3.82 | -0.63 | $a$ |
| $\mathrm{CH}_{3} \mathrm{CN}$ $=\mathrm{CH}-\mathrm{CN}$ | 2.63 2.97 | 3.92 3.87 | -1.29 | $a$ | $\mathrm{N}_{2} \mathrm{O}$ HONO | 0.76 | 0.17 | +0.59 | a |
| $\mathrm{CH}_{2}=\mathrm{CH}-\mathrm{CN}$ $\mathrm{CH} \equiv \mathrm{C}-\mathrm{CN}$ | 2.97 | 3.87 3.72 | -0.90 | $a$ | HONO trans | 2.27 | 1.86 | +0.41 | ? |
| $\mathrm{CH} \equiv \mathrm{C}-\mathrm{CN}$ | 3.21 | 3.72 | -0.51 | $a$ | HONO cis | 1.56 | 1.42 | +0.14 | $i$ |
| $\mathrm{CH}_{3} \mathrm{NC}$ | 2.17 | 3.85 | -1.68 | $a$ | $\mathrm{HONO}_{2}$ | 2.78 | 2.17 | +0.61 | $a$ |

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Table XIV. Net Atomic Charges $q_{X}{ }^{a}$

| Molecule | Atom X | $q_{\mathrm{X}}$, le ${ }^{\text {l }}$ | Molecule | Atom X | 9 X , lel |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CH}_{4}$ | C | +0.072 | $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{O}$ | C | +0.196 |
| $\mathrm{C}_{2} \mathrm{H}_{6}$ | C | +0.018 | ( $\left.\mathrm{CH}_{3}\right)_{2}$ | 0 | -0.335 |
| $\mathrm{C}_{2} \mathrm{H}_{4}$ | C | -0.084 | CO | C | +0.184 |
| $\mathrm{C}_{2} \mathrm{H}_{2}$ | C | -0.157 | $\mathrm{CO}_{2}$ | C | +0.446 |
| $\square$ | C | -0.077 | $\mathrm{CH}_{2} \mathrm{O}$ | C | +0.289 |
| $\square$ | C | -0.035 |  | ${ }^{\mathrm{O}}$ | -0.291 +0.349 |
| $\bigcirc$ | C | -0.059 | H-C | C $\mathrm{O}^{1}$ $\mathrm{O}^{2}$ | +0.349 -0.355 |
| $\mathrm{NH}_{3}$ | N | -0.246 | $\mathrm{O}^{2}-\mathrm{H}^{4}$ | $\mathrm{H}^{3}$ | -0.276 +0.081 |
| HCN | H | +0.191 |  | $\mathrm{H}^{4}$ | +0.081 +0.202 |
|  | C | -0.090 | $\mathrm{N}^{1}=\mathrm{N}^{2}=\mathrm{O}$ | $\mathrm{N}^{1}$ | -0.062 |
|  | N | -0.101 | N | $\mathrm{N}^{2}$ | +0.335 |
| $\begin{aligned} & \mathrm{H}_{2} \mathrm{O} \\ & \mathrm{CH}_{3} \mathrm{OH} \end{aligned}$ | ${ }_{0}^{\circ}$ | -0.318 +0.186 |  | 0 | -0.273 |
| $\mathrm{CH}_{3} \mathrm{OH}$ | C | $\begin{aligned} & +0.186 \\ & -0.327 \end{aligned}$ |  |  |  |

[^1] $P_{\mu \mu}$ is a diagonal element of the bond order matrix, and the summation extends over all basis orbitals of atom $\mathbf{X}$.
of MNDO over MINDO/3 are found in cases where directional effects play an important role. These improvements are especially pleasing in view of the facts that MNDO uses considerably fewer adjustable parameters than MINDO/ 3 and that the computational effort for MNDO is only slightly higher
than for MINDO/3.
MNDO therefore seems to represent a significant advance over MINDO/3, especially for compounds containing heteroatoms. Since MINDO/3 has already proved useful in a number of chemical connections, ${ }^{16}$ it seems likely that MNDO

Table XV. Computation Times $T$ for One SCF Calculation ${ }^{a}$

|  | $T . \mathrm{s}$ |  |  |  |
| :--- | :---: | :---: | ---: | ---: |
| Molecule | MINDO/3 | MNDO | STO-3G ${ }^{b}$ | $4-31 \mathrm{G}^{b}$ |
| $\mathrm{CH}_{4}$ | 0.44 | 0.53 | 4.60 | 22.07 |
| $\mathrm{C}_{2} \mathrm{H}_{6}$ | 1.65 | 1.98 | 26.09 | 155.91 |
| $\mathrm{C}_{3} \mathrm{H}_{8}$ | 3.11 | 4.21 | 93.79 |  |
| $\bigcirc \bigcirc$ | 6.59 | 7.16 | 255.56 | 1759.8 |
| $\bigcirc$ | 39.14 | 48.97 | 1279.0 |  |

${ }^{a}$ Central processor time on a CDC 6600 . The STO-3G and 4-31G programs were provided by Dr. A. Komornicki. ${ }^{b}$ On tlie CDC system, the user is additionally charged for the disk storage of integrals which amounts to about $40 \%$ of the total TM charges.
will find numerous applications in the study of reaction mechanisms and other chemical behavior.

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# Effect of Electronic State of Carbon Atoms on Their Reactions with Cyclopentadiene in Inert Gas Moderated Systems 

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#### Abstract

Products of the reactions of hot and moderated free carbon atoms with cyclopentadiene have been studied in pure and oxygen scavenged systems. Experiments with different rare gas moderators have provided evidence that both triplet and singlet carbon atoms react with cyclopentadiene and oxygen with comparable efficiencies and many similar products result. In distinction from previous work on oxygen scavenged alkane systems, acetylene is thought to be formed to some extent by thermal or near thermal $\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ atoms. The formation of the ring expansion product, benzene, also appears to result in part from $\mathrm{C}\left({ }^{( } \mathrm{P}\right)$ reactions. On the other hand, the straight chain $\mathrm{C}_{6} \mathrm{H}_{6}$ isomers are attributed almost exclusively to singlet atoms.


In the past decade as the result of the application of a variety of techniques, ${ }^{2}$ the broad outlines of the chemistry of the free carbon atom have been traced. Insertion into the $\mathrm{C}-\mathrm{H}$ bond, addition to the $\pi$ bond, and abstraction of oxygen and halogen atoms have all been identified. ${ }^{13}$ While some progress has been made in understanding the effects of excess kinetic energy on carbon atom reactivity, the problem is complex because of the need to sort out the effects of electronic excitation from those due to translational energy. This in turn is complicated by the fact that our knowledge of the differences in the chemistry of the ground $C\left({ }^{3} \mathrm{P}\right)$ and low-lying $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ and $\mathrm{C}\left({ }^{1} \mathrm{~S}\right)$ states is rudimentary. Some progress in unraveling these problems have been made recently as the result of a series of experiments involving production of C atoms by flash photolysis of $\mathrm{C}_{3} \mathrm{O}_{2}$ in the presence of simple substrates. ${ }^{3}$ The decay of these atoms was followed spectroscopically and rate constants were deduced. This work has shown that the $\mathrm{C}\left({ }^{( } \mathrm{D}\right)$ atom
reacts efficiently with both methane and ethylene. Acetylene is a major product of the methane reaction in agreement with earlier results of experiments with nucleogenic carbon atoms. ${ }^{13}$ The $\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ atom appears to react slowly with methane, and there is evidence from microwave discharge experiments with $\mathrm{C}_{3} \mathrm{O}_{2}$ that its reaction with ethylene is also slow. ${ }^{6}$ Such information is of considerable value in the interpretation of more complex systems.

Also of significance is the finding of Peterson ${ }^{14}$ that the choice of rare gas used as moderator in the nucleogenic experiments has a marked effect on triplet/singlet atom ratio, which varies from about 0.45 with neon to 2.3 or more with krypton and xenon. Taylor, Ache, and Wolf ${ }^{15}$ have also carried out moderation experiments in oxygen scavenged alkane systems. Their results have lead to the proposals that hot $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ forms methyne, hot $\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ and thermal $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ lead to acetylene, and thermal $\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ reacts $10^{4}$ to $10^{6}$ times faster with


[^0]:    ${ }^{a}$ Bond lengtlı $\mathrm{A}^{i} \mathrm{~B}^{j}$ (in $\AA$ ), bond angle $\mathrm{A}^{i} \mathrm{~B}^{j} \mathrm{C}^{k}$ (in deg), and dihedral angle $\mathrm{A}^{i} \mathrm{~B}^{j} \mathrm{C}^{k} \mathrm{D}^{l}$ (in deg) of $\mathrm{A}-\mathrm{B}$ witli respect to $\mathrm{C}-\mathrm{D}$ measured counter-

[^1]:    ${ }^{a}$ The net atomic charge $q_{\mathrm{X}}$, in units of the elementary charge lel, is defined as $q_{\mathrm{X}}=Z_{\mathrm{X}}-\Sigma_{\mu}{ }^{\mathrm{X}} P_{\mu \mu}$, where $Z_{\mathrm{X}}$ is the core charge of atom X ,

